

# Branching Input Strongest Typing Judgment

$$P = a? \{1_j(x_j) = P_j\}_{j \in J}$$

- ⑥ Let  $\emptyset; \Gamma_1^* \cup \{x_j\}_1; \emptyset; \Gamma_{(j)_u} \vdash_R P_j$  be the strongest judgment for  $P_j$ . (By induction,  $\exists! \Gamma_1^*$ )
- ⑥ Let  $\Delta_1; \Gamma_1; \Delta_u; \Gamma_u \vdash_R P$  be any judgment for process  $P$ . (R-INP)  $\Rightarrow \Delta_1 = \{a\}_1, \Gamma_1 = \Gamma_1^*, \Delta_u = \emptyset$  and  $\forall j \in J, \emptyset; \Gamma_1^* \cup \{x_j\}_1; \emptyset; \Gamma_u \cup \{x_j\}_u \vdash_R P_j$ .
- ⑥ By induction hypothesis :  $\forall j \in J, \Gamma_{(j)_u} \subseteq \Gamma_u \cup \{x_j\}_u$ .
- ⑥ Therefore :  $\bigcup_{j \in J} (\Gamma_{(j)_u} \setminus \{x_j\}_u) \subseteq \Gamma_u$ .
- ⑥ The strongest judgment for  $P$  is then :  
 $\{a\}_1; \Gamma_1^*; \emptyset; \bigcup_{j \in J} (\Gamma_{(j)_u} \setminus \{x_j\}_u) \vdash_R a? \{1_j(x_j) = P_j\}_{j \in J}$

# ***What Is TyCO, After All ?***

Maxime Gamboni

EPFL

# Asynchronous $\pi$ -Calculus

## Basic Components

- ⑥ Names :  $a, b, c, x \dots$
- ⑥ Processes :  $P, Q, \dots$

Processes use names as *channels* for sending or receiving data

- ⑥ Sending  $x$  on  $a$  :  $a!x$
- ⑥ Receiving  $x$  on  $a$  (and then processing it in  $P$ ) :  $a?(x).P$

# Asynchronous $\pi$ -Calculus (continued)

Processes can be combined using *parallel composition*

- ⑥  $P|Q$

Example :

- ⑥  $(a!x)|(a?(y).y!b) \rightarrow \mathbf{0}|x!b$

Names can be *restricted* to a part of a process

- ⑥  $((\nu x) P)|Q$  :  $x$  is visible in  $P$  but not (directly) in  $Q$

- ⑥  $((\nu x) a!x)|(a?(y).y!b) \rightarrow (\nu x) (\mathbf{0}|x!b)$  :  $P$  sends  $x$  on a name visible to  $Q$ , which *extrudes* the scope of  $x$ .

# $\pi_a^V$ : **Asynchronous $\pi$ -Calculus with Variants**

Names sent on a channel can be *labeled* :

⑥ in  $a!v$ ,

⑥  $v ::= a$  name  
|  $l\langle v \rangle$  labeled value

⑥ Labels are *not* names, they are just labels.

A *case destructor* can be used when receiving a labeled value :

⑥ case  $v$  of  $\{l_j(x_j) = P_j\}_{j \in J}$

# What is TyCO?

With slight syntactic changes, TyCO is just a sub-calculus of  $\pi_a^V$ :

- ⑥ Any output must be with a name having a single label (no label-nesting)
- ⑥ At input time the case destruction is done immediately.
- ⑥ Additionally, instead of writing  $a?(v).\text{case } v \text{ of } \{l_j(x_j)=P_j\}_{j \in J}$  like we would in  $\pi_a^V$ , we write  $a?\{l_j(x_j)=P_j\}_{j \in J}$ , which illustrates the atomicity of input and case-destruction.

# Example : Church-Encoding of Natural Numbers

- ⑥  $\mathbf{Zero}(x) \stackrel{\text{def}}{=} x?*\{q(a)=a!z\langle x\rangle\}$  (let  $x$  be the number zero)
- ⑥  $\mathbf{Succ}(y, x) \stackrel{\text{def}}{=} x?*\{q(a)=a!s\langle y\rangle\}$  (let  $x$  be the successor of  $y$ )
- ⑥  $\mathbf{Add}(x, y, z) \stackrel{\text{def}}{=} x!q(\nu a).a?\{z(b)=z!a\langle y\rangle,$   
 $s(b)=(\nu t) \mathbf{Add}(b, y, t)|$   
 $t?\{a(n)=z!a(\nu r).\mathbf{Succ}(n, r)\}$   
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# Is $\pi_a^V$ More Expressive than TyCO?

- ⑥ TyCO being a sub-calculus of  $\pi_a^V$ , an encoding of TyCO into  $\pi_a^V$  is straightforward.
- ⑥ Is it possible however to make an encoding of  $\pi_a^V$  into TyCO?
- ⑥ We need to encode nested variants as single-level variants and break the input / variant-destruction atomicity
- ⑥ The encoding needs to respect the process equivalences, i.e.  $P \mathcal{R} Q \Leftrightarrow \llbracket P \rrbracket \mathcal{R} \llbracket Q \rrbracket$



# Description of my project

- ⑥ To write a description of TyCO- $\pi_a^V$  encoding and prove it is valid
- ⑥ My guide @ EPFL provided me with a  $\pi_a^V$ -TyCO encoding
- ⑥ The goal of my project is to prove that it is valid and maybe to make necessary changes to it
- ⑥ If I have enough time, then study whether *Non-Uniform TyCO* can be encoded into  $\pi_a^V$

***That's All, Folks***

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